

Variables:

$d_o$  = object distance

$d_i$  = image distance (negative if behind mirror)

$h_o$  = object height

$h_i$  = image height (negative if inverted)

Equations

$$\frac{1}{f} = \frac{1}{d_o} + \frac{1}{d_i} \text{ or } f^{-1} = d_o^{-1} + d_i^{-1}$$

$$M = \frac{h_i}{h_o} = \frac{-d_i}{d_o}$$

Calculations with Concave Converging & Convex Diverging Mirrors

1. An object is 30.0 cm from a concave mirror of 15.0-cm focal length. The object is 1.8 cm high. Use the lens/mirror equation to answer the following:

a) Where is the image located?

$$\begin{aligned} d_o &= 30 \text{ cm} \\ f &= 15 \text{ cm} \\ h_o &= 1.8 \text{ cm} \\ d_i &=? \\ h_i &=? \end{aligned} \quad \begin{aligned} \frac{1}{f} &= \frac{1}{d_o} + \frac{1}{d_i} \\ \frac{1}{15} &= \frac{1}{30} + \frac{1}{d_i} \\ \frac{1}{15} - \frac{1}{30} &= \frac{1}{d_i} \\ \frac{2}{30} - \frac{1}{30} &= \frac{1}{d_i} \\ \frac{1}{30} &= \frac{1}{d_i} \end{aligned}$$

$$\boxed{d_i = 30 \text{ cm}}$$

b) How high is the image?

$$\begin{aligned} \frac{h_i}{h_o} &= \frac{-d_i}{d_o} \\ \frac{h_i}{1.8} &= \frac{-30}{30} \\ \frac{h_i}{1.8} &= -1 \end{aligned}$$

$$\boxed{h_i = -1.8 \text{ cm}}$$

negative means inverted

2. An object is placed 25.0 cm away from a concave mirror that has a focal length of 5.00 cm.

a) Where is the image located?

$$\begin{aligned} d_o &= 25 \text{ cm} \\ f &= 5 \text{ cm} \\ d_i &=? \end{aligned} \quad \begin{aligned} \frac{1}{f} &= \frac{1}{d_o} + \frac{1}{d_i} \\ \frac{1}{5} &= \frac{1}{25} + \frac{1}{d_i} \\ \frac{1}{5} - \frac{1}{25} &= \frac{1}{d_i} \\ \frac{5}{25} - \frac{1}{25} &= \frac{1}{d_i} \\ \frac{4}{25} &= \frac{1}{d_i} \end{aligned}$$

$$\boxed{d_i = 6.25 \text{ cm}}$$

b) If the object is 8.0 cm high, what is the height of the image?

$$\begin{aligned} \frac{h_i}{h_o} &= \frac{-d_i}{d_o} \\ \frac{h_i}{8} &= \frac{-(6.25)}{25} \end{aligned}$$

$$\frac{h_i}{8} = -0.25$$

$$\boxed{h_i = 2 \text{ cm}}$$

3. A convex security mirror in a warehouse has a radius of curvature of -1.0 m. A 2.0-m-high forklift is 5.0 m from the mirror.

$$r = -1 \text{ m} \rightarrow f = -0.5 \text{ cm}$$

a) What is the location of the image?

$$\begin{aligned} f &= -0.5 \text{ m} \\ h_o &= 2 \text{ m} \\ d_o &= 5.0 \text{ m} \\ d_i &=? \end{aligned} \quad \begin{aligned} \frac{1}{f} &= \frac{1}{d_o} + \frac{1}{d_i} \\ -\frac{1}{0.5} &= \frac{1}{5} + \frac{1}{d_i} \\ \frac{1}{d_i} &= -\frac{1}{0.5} - \frac{1}{5} \\ \frac{1}{d_i} &= -2.2 \end{aligned}$$

$$\boxed{d_i = -0.45 \text{ m}}$$

b) What is the size of the image?

$$\begin{aligned} \frac{h_i}{h_o} &= \frac{-d_i}{d_o} \\ \frac{h_i}{2} &= \frac{-(-0.45)}{5} \end{aligned}$$

$$\boxed{h_i = 0.18 \text{ m}}$$